# CODE

## P1-17-6-4



## Time : 3 Hours

## READ THE INSTRUCTIONS CAREFULLY

### GENERAL

- This sealed booklet is your Question Paper. Do not break the seal till you are told to do so.
- comer of the back cover of this booklet.
- 3. Use the Optical Response Sheet (ORS) provided separately for answering the questions.
- contact the invigilator for change of ORS.
- Blank spaces are provided within this booklet for rough work. 5.
- 6. booklet.
- for replacement of the booklet.
- You are allowed to take away the Question Paper at the end of the examination.

## OPTICAL RESPONSE SHEET

- The Candidate's Sheet is a carbon-less copy of the ORS.
- 10. Darken the appropriate bubbles on the ORS by applying sufficient pressure. This will leave an Impression at the corresponding place on the Candidate's Shoet.
- 11. The ORS will be collected by the invigilator at the end of the examination.
- 12. You will be allowed to take away the Candidate's Sheet at the end of the examination.
- Do not lamper with or mutilate the ORS. Do not use the ORS for rough work.
- 14. Write your name, roll number and code of the examination center, and sign with pen in the else on the ORS. Darken the appropriate bubble under each digit of your roll number.

## DARKENING THE BUBBLES ON THE ORS

- Use a BLACK BALL POINT PEN to darken the bubbles on the ORS.
- 16. Darken the bubble ( ) COMPLETELY.
- 17. The correct way of darkening a bubble is as :
- 18. The ORS is machine-gradable. Ensure that the bubbles are darkened in the correct way.
- "un-darken" a darkened bubble.



QUESTION PAPER FORMAT AND MARKING SCHEME

20. The question paper has three parts: Physics, Chemistry and Mathematics.

21. Each part has three sections as detailed in the following table:

	0		Cate	Category-wise Marks for Each Question					
Section	Type	Questions	Full Marks	Partial Marks	Zero Marks	Negative Marks	Marks of the Section		
1	One or more correct option(s)	7	+4 If only the bubble(s) corresponding to all the correct option(s) Is(ere) darkened	+1 For darkening a bubble corresponding to each correct option, provided NO incorrect option Is darkened	0 If none of the bubbles is darkened	-2 In all other cases	28		
2	Single digit Integer (0-9)	5	+3 If only the bubble corresponding to the correct answer is darkened	-	0 In ell othor cases	-	15		
3	Single Correct Option	6	+3 If only the bubble corresponding to the correct option is darkened	_	0 If none of the bubbles is darkened	-1 In all other cases	18		

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PAPER-1



#### Maximum Marks: 183

BY THE INVIGILATOR

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WITHOUT BEING INSTRUCTED TO

SEALS

BREAK THE

DO NOT

The paper CODE is printed on the right hand top corner of this sheet and the right hand top.

The paper CODE is printed on the left part as well as the right part of the ORS. Ensure that both these codes are identical and same as that on the question paper booklet. If not,

Write your name, roll number and sign in the space provided on the back cover of this

7. After breaking the seal of the booklet at 9:00 am, verify that the booklet contains 36 pages and that all the 54 questions along with the options are legible. If not, contact the invigilator

The ORS (top sheet) will be provided with an attached Candidate's Sheet (bottom sheet).

space provided for this purpose on the ORS. Do not write any of these details anywhere

19. Darken the bubbles ONLY IF you are sure of the answer. There is NO WAY to erase or

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SPACEFOR ROUGH WORK

#### PART I : PHYSICS

		SECTION 1 (Maximum Marks: 28)
<ul> <li>This section conta</li> </ul>	ins SEV	EN questions
<ul> <li>Each question has these four options</li> </ul>	FOUR is(are) c	options [A], [B], [C] and [D]. ONE OR MORE THAN ONE of orrect
<ul> <li>For each question,</li> </ul>	darken	the bubble(s) corresponding to all the correct option(s) in the ORS
<ul> <li>For each question,</li> </ul>	marks v	vill be awarded in one of the following categories:
<ul> <li>For each question, Full Marks</li> </ul>	marks v : +4	vill be awarded in one of the following categories: If only the bubble(s) corresponding to all the correct option(s) is(are) darkened
<ul> <li>For each question, Full Marks</li> <li>Partial Marks</li> </ul>	marics v : +4 : +1	vill be awarded in one of the following categories: If only the bubble(s) corresponding to all the correct option(s) is(are) darkened For darkening a bubble corresponding to each correct option provided NO incorrect option is darkened
<ul> <li>For each question, Full Marks Partial Marks Zera Marks</li> </ul>	marks v : +4 : +1 : 0	vill be awarded in one of the following categories: If only the bubble(s) corresponding to all the correct option(s, is(are) darkened For darkening a bubble corresponding to each correct option provided NO incorrect option is darkened If none of the bubbles is darkened

 For example, if [A], [C] and [D] are all the correct options for a question, darkening all these three will get +4 marks; darkening only [A] and [D] will get +2 marks; and darkening [A] and [B] will get -2 marks, as a wrong option is also darkened

Space for rough work

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If the thermal vertically at the bottom end of a uniform rope of constant mass per unit is the top and of the rope is attached to a fixed rigid support at O. A transverse wave is transverse wavelength  $\lambda_0$  is produced at point O on the rope. The pulse takes time is transverse wave pulse of wavelength  $\lambda_0$  is produced at point A (Pulse 2) the bost of M it takes time  $T_{AO}$  to reach point O. Which of the interval of M is takes time  $T_{AO}$  to reach point O. Which of the interval of M is takes time  $T_{AO}$  to reach point O.



- The velocities of the two pulses (Pulse 1 and Pulse 2) are the same at the midpoint of
- The velocity of any pulse along the rope is independent of its frequency and
- If I of The wavelength of Pulse 1 becomes longer when it reaches point A
- 101 The line Trot Tox

Space for rough work

Q.2 A circular insulated copper wire loop is twisted to form two loops of area A and 2A as shown in the figure. At the point of crossing the wires remain electrically insulated from each other. The entire loop lies in the plane (of the paper). A uniform magnetic field  $\vec{B}$  points into the plane of the paper. At t = 0, the loop starts rotating about the common diameter as axis with a constant angular velocity  $\omega$  in the magnetic field. Which of the following options is/are correct?



- [A] The net emf induced due to both the loops is proportional to cos wt
- [P] The rate of change of the flux is maximum when the plane of the loops is perpendicular to plane of the paper

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- [C] The amplitude of the maximum net emf induced due to both the loops is equal to the amplitude of maximum emf induced in the smaller loop alone
- [D] The emf induced in the loop is proportional to the sum of the areas of the two loops

Space for rough work

Q.3 A block of mass *M* has a circular cut with a frictionless surface as shown. The block rests on the horizontal frictionless surface of a fixed table. Initially the right edge of the block is at x = 0, in a *co-ordinate system fixed to the table*. A point mass *m* is released from rest at the topmost point of the path as shown and it slides down. When the mass loses contact with the block, its position is *x* and the velocity is *v*. At that instant, which of the following options is/arc correct?



Space for rough work

- Q.4 A flat plate is moving normal to its plane through a gas under the action of a constant force F. The gas is kept at a very low pressure. The speed of the plate v is much less than the average speed u of the gas molecules. Which of the following options is/are true?
  - [A] The pressure difference between the leading and trailing faces of the plate is proportional to we
  - [B] At a later time the external force F balances the resistive force
  - [2] The resistive force experienced by the plate is proportional to v
  - [D] The plate will continue to move with constant non-zero acceleration, at all times
- Q.5 In the circuit shown,  $L = 1 \mu H$ ,  $C = 1 \mu F$  and  $R = 1 k\Omega$ . They are connected in series with an a.c. source  $V = V_0 \sin \omega t$  as shown. Which of the following options is/are correct?  $L = 1 \mu H$   $C = 1 \mu F$   $R = 1 k\Omega$



- [A] The current will be in phase with the voltage if  $\omega = 10^4$  rad. s<sup>-1</sup>
- [B] At  $\omega \gg 10^6$  rad. s<sup>-1</sup>, the circuit behaves like a capacitor
- [9] The frequency at which the current will be in phase with the voltage is independent of R

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[D] At ω~0 the current flowing through the circuit becomes nearly zero

Space for rough work

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Q.6 For an isosceles prism of angle A and refractive index  $\mu$ , it is found that the angle of minimum deviation  $\delta_m = A$ . Which of the following options is/are correct?

[A] At minimum deviation, the incident angle  $l_1$  and the refracting angle  $r_1$  at the first refracting surface are related by  $r_1 = (i_1/2)$ 

- [B] For this prism, the refractive index  $\mu$  and the angle of prism A are related as  $A = \frac{1}{2} \cos^{-1} \left(\frac{\mu}{2}\right)$
- $\int \mathcal{O} \quad \vec{F} \partial t$  the angle of incidence  $l_1 = A$ , the ray inside the prism is parallel to the base of the prism
- [D] For this prism, the emergent ray at the second surface will be tangential to the surface when the angle of incidence at the first surface is  $i_{1} = \sin^{-1} \left[ \sin A \sqrt{4 \cos^{2} \frac{A}{2} 1} \cos A \right]$
- Q.7 A human body has a surface area of approximately 1 m<sup>2</sup>. The normal body temperature is 10 K above the surrounding room temperature  $T_0$ . Take the room temperature to be  $T_0 = 300$  K. For  $T_0 = 300$  K, the value of  $\sigma T_0^4 = 460$  Wm<sup>-2</sup> (where  $\sigma$  is the Stefan-Boltzmann constant). Which of the following options is/are correct?
  - [A] If the surrounding temperature reduces by a small amount  $\Delta T_0 \ll T_0$ , then to maintain the same body temperature the same (living) burnan being needs to radiate  $\Delta W = 4\sigma T_0^3 \Delta T_0$  more energy per unit time
  - [B] Reducing the exposed surface area of the body (e.g. by curling up) allows humans to maintain the same body temperature while reducing the energy lost by radiation
  - [C] If the body temperature rises significantly then the peak in the spectrum of clectromagnetic radiation emitted by the body would shift to longer wavelengths
  - [D] The amount of energy radiated by the body in 1 second is close to 60 Joules

Space for rough work



Q.8 A drop of liquid of radius  $R = 10^{-2}$  m having surface tension  $S = \frac{0.1}{4\pi}$  Nm<sup>-1</sup> divides itself

(a) into K identical drops. In this process the total change in the surface energy  $\Delta U = 10^{-3}$  J. If  $K = 10^{\alpha}$  then the value of  $\alpha$  is

- Q.9 A monochromatic light is travelling in a medium of refractive index n = 1.6. It enters a stack of glass layers from the bottom side at an angle  $\theta = 30^{\circ}$ . The interfaces of the glass
- (c) layers are parallel to each other. The refractive indices of different glass layers are monotonically decreasing as  $n_m = n m\Delta n$ , where  $n_m$  is the refractive index of the  $m^{th}$  slab and  $\Delta n = 0.1$  (see the figure). The ray is refracted out parallel to the interface between the  $(m-1)^{th}$  and  $m^{th}$  slabs from the right side of the stack. What is the value of m?



#### Space for rough work

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		SECTION 3 (Maximum Marks: 18)
This section	contains SI	X questions of matching type
This section	contains T	WO tables (each having 3 columns and 4 rows)
· Based on eac	h table, the	ere are THREE questions
• Each questio	n has FOL	R options [A], [B], [C], and [D]. ONLY ONE of these four options
· For each que	stion, dark	en the bubble corresponding to the correct option in the ORS
• For each que	stion, mark	s will be awarded in one of the following categories:
Full Marks	: +3 : 0	If only the bubble corresponding to the correct option is darkened If none of the bubbles is darkened
Negative M	arks: -1	In all other cases

Space for rough work

## Answer Q.13, Q.14 and Q.15 by appropriately matching the information given in the three columns of the following table.

A charged particle (electron or proton) is introduced at the origin (x = 0, y = 0, z = 0) with a given initial velocity  $\vec{v}$ . A uniform clectric field  $\vec{E}$  and a uniform magnetic field  $\vec{B}$  exist everywhere. The velocity  $\vec{v}$ , electric field  $\vec{E}$  and magnetic field  $\vec{B}$  are given in columns 1, 2 and 3, respectively. The quantities  $E_0, B_0$  are positive in magnitude.

Column 1	Column 2	Column 3	
(I) Electron with $\vec{v} = 2 \frac{\epsilon_0}{B_0} \hat{x}$	(i) $\vec{E} = E_0 \hat{z}$	$(\mathbf{P}) \ \vec{B} = -B_0 \hat{\mathbf{x}}$	
(II) Electron with $\vec{v} = \frac{E_0}{B_0} \hat{y}$	(ii) $\vec{E} = -E_0 \hat{\mathcal{Y}}$	$(\mathbf{Q}) \ \vec{B} = B_0 \hat{\mathbf{x}}$	
(III) Proton with $\vec{v} = 0$	(iii) $\vec{E} = -E_0 \hat{X}$	(R) $\vec{B} = B_0 \hat{y}$	
(IV) Proton with $\vec{v} = 2 \frac{\vec{E}_0}{\vec{E}_0} \hat{x}$	(iv) $\vec{E} = E_0 \hat{X}$	(S) $\vec{B} = B_0 \hat{z}$	

Q.13 In which case will the particle move in a straight line with constant velocity?

#### [A] (IV) (i) (S) [B] (III) (ii) (R) [C] (II) (iii) (S) [D] (III) (iii) (P)

Q.14 In which case will the particle describe a helical path with axis along the positive z direction?

[A] (IV) (i) (S)	[B] (II) (ii) (R)	[C] (III) (iii) (P)	[DP] (IV) (ii) (R)
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Q.15 In which case would the particle move in a straight line along the negative direction of yaxis (i.e., move along - 9)?

[A] (III) (ii) (R) [B] (IV) (ii) (S) [Q] (III) (ii) (P) [D] (II) (iii) (Q)

Space for rough work

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An ideal gas is undergoing a cyclic thermodynamic process in different ways as shown in the corresponding P - V diagrams in column 3 of the table. Consider only the path from state 1 to state 2. W denotes the corresponding work done on the system. The equations and plots in the table have standard notations as used in thermodynamic processes. Here y is the ratio of heat capacities at constant pressure and constant volume. The number of moles in the gas is n.



Space for rough work

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	1	18-12	19.4						
هل	10	II) (iii) (	P)	[B]	(II) (iii) (S)	[C]	(III) (iii) (P)	[D]	(II) (iv) (R)
Q.17 W	hich	one of t	the foll	lowing	options is the c	orrect o	combination?		
[A	] (	l) (iv) (	P)	(B)	(IV) (ii) (S)	[C]	(II) (iv) (R)	101	(III) (ii) (S)
Q.18 W us	hich ed a	one of a corre	the fo	llowing n the de	options correctermination of	ctly rep the spe	resents a therm ed of sound in a	iodynan an ideal	nic process that l gas?
6	10	II) (iv) (	(R)	[B]	(I) (ii) (Q)	[C]	(IV) (ii) (R)	por	(l) (iv) (Q)
				E	ND OF PART	<b>[]:P</b> B	IYSICS		
					Space for re	ough w	rork	1	1.
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#### **PART II : CHEMISTRY**

#### SECTION 1 (Maximum Marks: 28)

This section contains SEVEN questions

- Each question has FOUR options [A], [B], [C] and [D]. ONE OR MORE THAN ONE of these four options is(are) correct
- For each question, darken the bubble(s) corresponding to all the correct option(s) in the ORS
- · For each question, marks will be awarded in one of the following categories:

1	Full Marks	:	+4	If only the bubble(s) corresponding to all the correct option(s)
ł				is(are) darkened
ſ.	Partial Marks	:	+1	For darkening a bubble corresponding to each correct option,
1				provided NO incorrect option is darkened
	Zero Marks	:	0	If none of the bubbles is darkened
	Negative Marks	1	-2	In all other cases

- For example, if [A], [C] and [D] are all the correct options for a question, darkening all these three will get +4 marks; darkening only [A] and [D] will get +2 marks; and darkening [A] and [B] will get -2 marks, as a wrong option is also darkened
- Q.19 An ideal gas is expanded from (p<sub>1</sub>, V<sub>1</sub>, T<sub>1</sub>) to (p<sub>2</sub>, V<sub>2</sub>, T<sub>2</sub>) under different conditions. The correct statement(s) among the following is(are)
  - [A] The work done by the gas is less when it is expanded reversibly from  $V_1$  to  $V_2$  under adiabatic conditions as compared to that when expanded reversibly from  $V_1$  to  $V_2$  under isothermal conditions
  - [B] The change in internal energy of the gas is (i) zero, if it is expanded reversibly with  $T_1 = T_2$ , and (ii) positive, if it is expanded reversibly under adiabatic conditions with  $T_1 \neq T_2$
  - $[\mathcal{C}]$  If the expansion is carried out freely, it is simultaneously both isothermal as well as adiabatic
  - [D] The work done on the gas is maximum when it is compressed irreversibly from  $(p_2, V_2)$  to  $(p_1, V_1)$  against constant pressure  $p_1$

Space for rough work

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Q.20 The IUPAC name(s) of the following compound is(are)

н₁с-{\_\_\_\_

[A] 4-methylchlorohenzenc [C] 1-chloro-4-methylbenzene 19 4-chlorotoluene

[D] 1-methyl-4-chlorobenzene

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Q.21 For a solution formed by mixing liquids L and M, the vapour pressure of L plotted against the mole fraction of M in solution is shown in the following figure. Here x<sub>L</sub> and x<sub>M</sub> represent mole fractions of L and M, respectively, in the solution. The correct statement(s) applicable to this system is(are)



- [44] The point Z represents vapour pressure of pure liquid M and Raoult's law is obcycd from  $x_L = 0$  to  $x_L = 1$
- [B] Attractive intermolecular interactions between L-L in pure liquid L and M-M in pure liquid M are stronger than those between L-M when mixed in solution
- [C] The point Z represents vapour pressure of pure liquid M and Raonit's law is obcycd when  $x_L \rightarrow 0$
- [D] The point 2 represents vapour pressure of pure liquid L and Raoult's law is obcycd when  $x_L \to 1$

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Q.22 The correct statement(s) for the following addition reactions is(are)

(i) 
$$H_3C \xrightarrow{H/_2} CH_3$$
  $H_{r_2}/CHCl_3$   $M \text{ and } N$   
(ii)  $H_3C \xrightarrow{CH_3} Br_2/CHCl_3$   $O \text{ and } P$ 

- [A] (M and O) and (N and P) are two pairs of enantiomers
- [B] Bromination proceeds through trans-addition in both the reactions
- [C] O and P are identical molecules
- [D] (M and O) and (N and P) are two pairs of diastereomers
- Q.23 Addition of excess aqueous ammonia to a pink coloured aqueous solution of MCl<sub>2</sub>·6H<sub>2</sub>O (X) and NH<sub>4</sub>Cl gives an octabedral complex Y in the presence of air. In aqueous solution, complex Y behaves as 1:3 electrolyte. The reaction of X with excess HCl at room temperature results in the formation of a blue coloured complex Z. The calculated spin only magnetic moment of X and Z is 3.87 B.M., whereas it is zero for complex Y. Among the following options, which statement(s) is(are) correct?
  - [A] The hybridization of the central metal ion in X is d<sup>2</sup>sp<sup>3</sup>
  - [B] Addition of silver nitrate to Y gives only two equivalents of silver chloride
  - [C] When X and Z are in equilibrium at 0°C, the colour of the solution is pink
  - D Z is a tetrahedral complex

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#### Q.24 The correct statement(s) about the oxoacids, HClO4 and HClO, is(are)

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[A] (The central atom in both HClO<sub>4</sub> and HClO is  $sp^3$  hybridized

[B] HClO4 is formed in the reaction between Cl2 and H2O

[C] The conjugate base of HClO4 is weaker base than H2O

DI HClO4 is more acidic than HClO because of the resonance stabilization of its anion

- Q.25 The colour of the X<sub>2</sub> molecules of group 17 elements changes gradually from yellow to violet dówn the group. This is due to
  - [A] decrease in  $\pi^* \sigma^*$  gap down the group

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- [B] decrease in ionization energy down the group
- $[\mathcal{Q}]$  the physical state of  $X_2$  at room temperature changes from gas to solid down the group
- [D] decrease in HOMO-LUMO gap down the group

Space for rough work



Space for rough work

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6: 1 de Q.28 Among  $H_2$ ,  $H_{2_2}^+$ ,  $L_{1_2}$ ,  $Be_1$ ,  $H_2$ ,  $C_2$ ,  $N_2$ ,  $O_2^-$ , and  $F_2$ , the number of diamagnetic species is (Atomic numbers: H = 1, He = 2, Li = 3, Be = 4, B = 5, C = 6, N = 7, O = 8, F = 9) SECTION 3 (Maximum Marks: 18) \* This section contains SIX questions of matching type O.29 A crystalline solid of a pure substance has a face-centred cubic structure with a cell edge of This section contains TWO tables (each having 3 columns and 4 rows) 400 pm. If the density of the substance in the crystal is 8 g cm<sup>-3</sup>, then the number of atoms · Based on each table, there are THREE questions present in 256 g of the crystal is  $N \times 10^{14}$ . The value of N is . Each question has FOUR options [A], [B], [C], and [D]. ONLY ONE of these four options is correct 0.30 The conductance of a 0.0015 M aqueous solution of a weak monobasic acid was determined by using a conductivity cell consisting of platinized Pt electrodes. The distance · For each question, darken the bubble corresponding to the correct option in the ORS between the electrodes is 120 cm with an area of cross section of 1 cm2. The conductance of this solution was found to be  $5 \times 10^{-7}$ S. The pH of the solution is 4. The value of · For each question, marks will be awarded in one of the following categories: limiting molar conductivity  $(\Lambda_{m}^{s})$  of this weak monobasic acid in aqueous solution is If only the bubble corresponding to the correct option is darkened Full Marks : +3  $Z \times 10^2$  S cm<sup>-1</sup> mol<sup>-1</sup>. The value of Z is Zero Marks : 0 If none of the bubbles is darkened Negative Marks: -1 In all other cases Space for rough work HAN BAN & = XX LOC Rall Hash

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	columns of the following table.					
The wave function, $\psi_{n,l,m}$ is a mathematical function polar coordinates $(r, \theta, \phi)$ of the electron and character	whose value depends upon spherical rized by the quantum numbers $n$ , $l$ and	Column respect	ns 1, 2 and 3 cont ively.	tain starting materials, reaction	conditions, and type of react	ions,
$m_i$ . Here r is distance from nucleus, $\theta$ is colatitude	and $\phi$ is azimuth. In the mathematical		Column 1	Column 2	Column 3	
nctions given in the Table, $Z$ is atomic number and	a, is Bohr radius.	(I) Tolu	uene	(i) NaOH/ Br <sub>2</sub>	(P) Condensation	-
Column 1 Column 2	Column 3	(LI) Acc	etophenone	(ii) Br <sub>2</sub> / hv	(Q) Carboxylation	
(i) $\psi_{a,b} = \alpha \left( \frac{Z}{2} \right)^2 e^{-\left( \frac{Z}{a_a} \right)}$		(III) Be	enzaldehyde	(iii) (CH <sub>3</sub> CO) <sub>2</sub> O/ CH <sub>3</sub> COOK	(R) Substitution	
(a, )	E	(IV) Pb	nenol	(iv) NaOH/ COz	(S) Haloform	
	$\begin{array}{c} {_{\scriptstyle E}} {_{\scriptstyle I'}} {_{\scriptstyle I''}} {_{\scriptstyle I''}} {_{\scriptstyle I''}} {_{\scriptstyle I''}} {_{\scriptstyle I'''}} {_{\scriptstyle I''''}} {_{\scriptstyle I''''''}} {_{\scriptstyle I''''''''''''''''''''''''''''''''''''$	Q.34 Th mo	conly CORREC	T combination in which the	reaction proceeds through r	adical
ID 2s orbital (ii) One radial node	(O) Probability density at nucleus	[^				
(1) One month hode	$\alpha \frac{1}{a^3}$ 1	Q.35 Fo	or the synthesis of be	enzoic acid, the only CORRECT	Combination is	
If) $2p_x$ orbital (iii) $\psi_{n,l,m} \propto \left(\frac{Z}{z}\right)^{\frac{5}{2}} re^{-\left(\frac{Z}{2a_x}\right)} \cos \theta$	(R) Probability density is maximum at nucleus	[A	.] (II) (i) (S) "	[B] (I) (iv) (Q) [C] (I <sup>V</sup>	V) (ii) (P) 🛛 🖓 (III) (iv) (R	)
$(a_o)$ $3d_z^2$ orbital (iv) xy-plane is a nodal plane	(S) Energy needed to excite	Q.36 Tb	ac only CORRECT	combination that gives two diffe	erent carboxylic acids is	
	electron from $n = 2$ state to $n =$	x]	イ (IV) (iii) (Q)	[B] (II) (iv) (R) [C] (I)	) (i) (S) [D] (Ш) (iii) (P)	)
	4 state is $\frac{21}{32}$ times the energy	¢.,		END OF PART II : CHEMI	ISTRY	
	n=2 state to $n=6$ state			Space for rough work		
2,31 For He <sup>+</sup> ion, the only INCORRECT combination	is					
[A] (I) (I) (S) [B] (II) (II) (Q) [C]	(1) (11) (R) [D] (1) (i) (R)	1				
.32 For the given orbital in Column 1, the only CORJ species is	ECT combination for any hydrogen-like					
[A] (II) (ii) (P) [B] (I) (ii) (S) [C]	(IV) (iv) (R) [D]. (UI) (iii) (P)					
For hydrogen atom, the only CORRECT combina	ion is					
[A] (Î) (i) (P) [B] (I) (iv) (R) [C]	(II) (i) (Q) <b>J</b> ØJ (I) (i) (S)			· 4 · · ·		
Space for rough	vork			· · · · · · · · ·		
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## Answer Q.31, Q.32 and Q.33 by appropriately matching the information given in the three

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Answer Q.34, Q.35 and Q.36 by appropriately matching the information given in the three



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#### **PART III : MATHEMATICS**

#### SECTION 1 (Maximum Marks: 28)

This section contains SEVEN questions

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- · Each question has FOUR options [A], [B], [C] and [D]. ONE OR MORE THAN ONE of these four options is(are) correct
- · For each question, darken the bubble(s) corresponding to all the correct optioo(s) in the ORS
- · For each question, marks will be awarded in one of the following eategories:

Full Marks	: +4	If only the hubble(s) corresponding to all the correct option(s)
Partial Marks	: +1	is(are) darkened For darkening a hubble corresponding to each correct option
Participant and a second second		provided NO incorrect option is darkened
Zera Marks	: 0	If none of the hubbles is darkened
Negative Marks	: -2	In all other cases

For example, if [A], [C] and [D] are all the correct options for a question, darkening all these three will get +4 marks; darkening only [A] and [D] will get +2 marks; and darkening [A] and [B] will get -2 marks, as a wrong option is also darkened

Q.3? Let X and Y be two events such that  $P(X) = \frac{1}{2}$ ,  $P(X|Y) = \frac{1}{2}$  and  $P(Y|X) = \frac{2}{5}$ . Then

$\int A \int P(Y) = \frac{4}{15}$	$[B] P(X' Y) = \frac{1}{2}$
$[C] P(X \cup Y) = \frac{2}{5}$	$[D]  P(X \cap Y) = \frac{1}{s}$

Q.38 Let  $f: \mathbb{R} \to (0, 1)$  be a continuous function. Then, which of the following function(s) bas(have) the value zero at some point in the interval (0, 1)?

	Space for rough work	$\frac{P(x + y)}{P(x)} = \frac{1}{2} = \frac{P(x + y)}{P(x)}$	PLY PL
$[C]  x - \int_0^{\frac{\pi}{2} x} f(t) \cos t  dt$	[D] x <sup>9</sup> -	f(x)	
$[A] e^x - \int_0^x f(t) \sin t  dt$	[B] <i>f</i> ( <i>x</i> )	$+\int_0^{\frac{\pi}{2}}f(t)\sin tdt$	

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for rough work 
$$\frac{P(x, ny)}{P(y)} = \frac{1}{2} \frac{A}{4} \frac{P(y, ny)}{P(y)} = \frac{2}{5}$$
  
 $\frac{P(x, ny)}{N/15} = \frac{P(y)}{15} = \frac{P(y)}{15} = \frac{P(y, ny)}{15} = \frac{2}{5x_{2}} = \frac{2}{15}$   
 $\frac{1-2}{15} \frac{11}{15} \frac{A}{x_{1}} = \frac{5}{15} + \frac{y}{15} = \frac{2}{15} = \frac{1-2}{15} \frac{A}{15} + \frac{15}{15} + \frac{2}{15}$ 

Q.39 Let a, b, x and y be real numbers such that a - b = 1 and  $y \neq 0$ . If the complex number z = x + iy satisfies  $Im\left(\frac{ax+b}{x+1}\right) = y$ , then which of the following is(are) possible value(s) of x7 Ux+ :08+ 5 ++1+18 , [A]  $1 - \sqrt{1 + y^2}$ ,  $[B] -1 - \sqrt{1 - y^2}$  $[p] -1 + \sqrt{1 - y^2}$ [C]  $1 + \sqrt{1 + y^2}$ 

Q.40 If 2x - y + 1 = 0 is a tangent to the hyperbola  $\frac{x^2}{a^2} - \frac{y^2}{16} = 1$ , then which of the following CANNOT be sides of a right angled triangle?

Q.41 Let [x] be the greatest integer less than or equals to x. Then, at which of the following point(s) the function  $f(x) = x \cos(\pi(x + [x]))$  is discontinuous?

$$[A] x = -1$$
 [B]  $x = 1$  [C]  $x = 0$  [D]  $x = 2$ 



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a

\* 4

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	Column 1	Column 2	Column 3
(I)	$x^2 + y^2 = a^2$	(i) $my = m^2x + a$	(P) $\left(\frac{\alpha}{m^2}, \frac{2a}{m}\right)$
(4)	$x^2 + a^2 y^2 = a^2$	(ii) $y = mx + a\sqrt{m^2 + 1}$	(Q) $\left(\frac{-ma}{\sqrt{m^2+1}}, \frac{a}{\sqrt{m^2+1}}\right)$
(111)	$y^2 = 4ax$	(iii) $y = mx + \sqrt{a^2 m^2 - 1}$	(R) $\left(\frac{-a^{2}m}{\sqrt{a^{2}m^{2}+1}}, \frac{1}{\sqrt{a^{2}m^{2}+1}}\right)$
(IV)	$x^2 - a^2 y^2 = a^2$	(iv) $y = mx + \sqrt{a^2m^2 + 1}$	(S) $\left(\frac{-a^2m}{\sqrt{a^2m^2-1}}, \frac{-1}{\sqrt{a^2m^2-1}}\right)$

## Answer Q.49, Q.50 and Q.51 by appropriately matching the information given in the three columns of the following table.

Q.49 For  $a = \sqrt{2}$ , if a tangent is drawn to a suitable conic (Column 1) at the point of contact (-1, 1), then which of the following options is the only CORRECT combination for obtaining its equation?

[1] (1) (i) (0) [8] (1) (i) (P) [C] (11) (i) (P) [1]	[D] (II) (ii) (O)
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## Q.50 The tangent to a suitable conic (Column 1) at $(\sqrt{3}, \frac{1}{2})$ is found to be $\sqrt{3}x + 2y = 4$ , then which of the following options is the only CORRECT combination?

[A<sup>A</sup>] (IV) (iv) (S) [D<sup>A</sup>] (II) (iv) (R) [C] (IV) (iii) (S) [D] (II) (iii) (R)

Q.51 If a tangent to a suitable conic (Column 1) is found to be y = x + 8 and its point of contact is (8, 16), then which of the following options is the only CORRECT combination?

	[K]	(III) (i) (P)	[B]	(I) (ii) (Q)	[C] (II) (iv) (R)	[D] (III) (ii) (Q)
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Space for rough work

## Answer Q.52, Q.53 and Q.54 by appropriately matching the information given in the three columns of the following table.

Let $f(x) = x + \log_e x - x \log_e x, x + \log_e x, x + \log_e x, x + \log_e x, x + \log_e x + $	$\in (0, \infty)$ . bout zeros of $f(x)$ , $f'(x)$ and bout the limiting behavior of $f$ bout increasing/decreasing nat	f''(x). f(x), f'(x) and $f''(x)$ at infinity. mre of $f(x)$ and $f'(x)$ .
Column 1	Column 2	Column 3
(1) $f(x) = 0$ for some $x \in (1, e^2)$	(i) $\lim_{x\to\infty} f(x) = 0$	$(\tilde{\mathbf{P}}) f$ is increasing in $(0, 1)$
(II) $f'(x) = 0$ for some $x \in (1, e)$	(ii) $\lim_{x\to\infty} f(x) = -\infty$	$(\hat{Q}) f$ is decreasing in $(e, e^2)$
(III) $f'(x) = 0$ for some $x \in (0, 1)$	(iii) $\lim_{x\to\infty} f'(x) = -\infty$	(R) $f'$ is increasing in (0, 1)
(IV) $f''(x) = 0$ for some $x \in (1, e)$	$(iv) \lim_{x\to\infty} f''(x) = 0$	(S) $f'$ is decreasing in $(e, e^2)$

Q.52 Which of the following options is the only INCORRECT combination?

[A] (I) (iii) (P)	[B] (II) (iv) (Q)	[C] (II) (iii) (P)	[10] (III) (i) (R
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#### Q.53 Which of the following options is the only CORRECT combination?

[A] (I)(ii)(R)	[B] .(III) (iv) (P)	[2] (U) (iii) (S)	(IV) (i) (S)
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#### Q.54 Which of the following options is the only CORRECT combination?

[A] (III) (iii) (R) [A] (IV) (iv) (S) [C] (II) (ii) (Q) [A] (I) (i) (P) END OF THE QUESTION PAPER

